

14

Answers to exercises

Chapter 1

Dioecious trees

The question is whether the number of flowers produced depends upon the sex of the tree. The variable `SEX` is categorical with two levels. The commands to execute the ANOVA are as before.

MINITAB COMMANDS FOR BOX 15.1 Analysis for dioecious trees

| | |
|------------|--|
| Commands | <code>anova FLOWERS = SEX.</code> |
| Menu route | Stat > ANOVA > Balanced ANOVA FLOWERS → Response SEX → Model |

This would produce the following output:

MINITAB OUTPUT FOR BOX 15.1 Analysis for dioecious trees

ANOVA: FLOWERS versus SEX

| Factor | Type | Levels | Values |
|--------|-------|--------|--------|
| SEX | fixed | 2 | 1 2 |

Analysis of Variance for FLOWERS

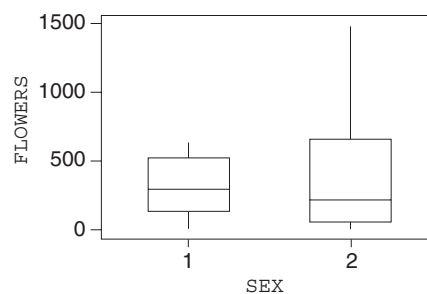
| Source | DF | SS | MS | F | P |
|--------|----|---------|--------|------|-------|
| SEX | 1 | 171841 | 171841 | 1.18 | 0.284 |
| Error | 48 | 7017255 | 146193 | | |
| Total | 49 | 7189097 | | | |

There are a number of ways in which these results could be illustrated graphically, one of which is a boxplot.

MINITAB COMMANDS FOR FIGURE 15.1 **Box plot for dioecious trees**

| | |
|------------|---|
| Commands | <code>boxplot FLOWERS*SEX</code> |
| Menu route | Graph > Boxplot FLOWERS → Graph variables, Y SEX → Graph variables, X |

This would produce the following graph:



Minitab Output for Fig. 15.1 Boxplot for dioecious trees

Chapter 2

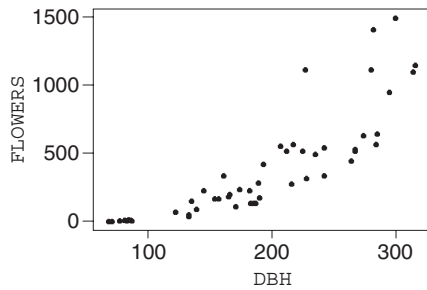
Dioecious trees

The variables FLOWERS and DBH are both continuous, so the best illustration of the relationship between them would be a scatter plot.

MINITAB COMMANDS FOR FIGURE 15.2 **Graph of FLOWERS versus DBH**

| | |
|------------|--|
| Commands | <code>plot FLOWERS*DBH</code> |
| Menu route | Graph > Plot FLOWERS → Graph variable, Y DBH → Graph variable, X |

This would produce the following graph:



Minitab output for Fig 15.2 Graph of FLOWERS versus DBH.

The regression analysis would be executed using the following commands:

| MINITAB COMMANDS FOR BOX 15.2 Analysis for dioecious trees | |
|--|--|
| Commands | <code>regress FLOWERS 1 DBH</code> |
| Menu route | Stat > Regression > Regression FLOWERS → Response DBH → Predictors |

which would give the following output:

| MINITAB OUTPUT FOR BOX 15.2 Analysis for dioecious trees | | | | | |
|--|--------------|-------------------|---------|--------|-------|
| Regression Analysis: FLOWERS versus DBH | | | | | |
| The regression equation is FLOWERS = - 481 + 4.51 DBH | | | | | |
| Predictor | Coef | SE Coef | T | P | |
| Constant | -481.16 | 86.24 | -5.58 | 0.000 | |
| DBH | 4.5128 | 0.4224 | 10.68 | 0.000 | |
| S = 210.6 | R-Sq = 70.4% | R-Sq(adj) = 69.8% | | | |
| Analysis of Variance | | | | | |
| Source | DF | SS | MS | F | P |
| Regression | 1 | 5060723 | 5060723 | 114.13 | 0.000 |
| Residual Error | 48 | 2128374 | 44341 | | |
| Total | 49 | 7189097 | | | |

Unusual Observations

| Obs | DBH | FLOWERS | Fit | SE Fit | Residual | St Resid |
|-----|-----|---------|-------|--------|----------|----------|
| 5 | 227 | 1107.0 | 543.3 | 33.3 | 563.7 | 2.71R |
| 28 | 300 | 1482.0 | 872.7 | 54.6 | 609.3 | 3.00R |
| 50 | 282 | 1398.0 | 791.5 | 48.4 | 606.5 | 2.96R |

R denotes an observation with a large standardized residual

Chapter 3

How variability in the population will influence our analysis

To create datasets for this exercise, just follow the procedure outlined in Box 3.3a ‘Creating your own datasets’, but alter the standard deviation specified when you draw the random numbers from the Normal distribution (third step in Minitab commands 3.3a). One advantage of using the command line method is that you can copy-and-paste the whole set of commands, edit the number you want to change, and then execute the whole lot by pressing the return key.

Each of the four created data sets can be analysed using the commands shown below:

MINITAB COMMANDS TO ANALYSE SIMULTATED DATA SETS

Commands `brief 3.`
 `glm Y = F.`

Menu route Stat > ANOVA > General Linear Model
 Y → Response
 F → Model

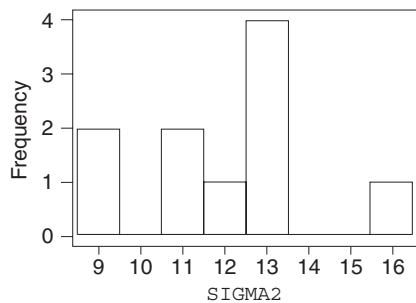
⊙ In addition, coefficients for all terms

Each analysis will produce one estimate of the grand mean, which may then be entered into a new column in the worksheet. When ten estimates have

been obtained, a histogram may be drawn for the column SIGMA2 (for example) using the commands:

| MINITAB COMMANDS TO PLOT HISTOGRAMS OF SIMULATED DATA | |
|---|---|
| Commands | <code>histogram SIGMA2</code> |
| Menu route | Graph > Histogram SIGMA2 → Graph variables |

This would produce a graph similar to the one below:



Minitab output for Fig 15.3 Variation of parameter estimates.

Comparison of the four graphs with the error standard deviation set at 2, 4, 8, and 16 will illustrate how the error variance will influence the reliability of the grand mean estimate.

Chapter 4

Investigating obesity

First you need to conduct two separate analyses to explain FOREARM using HT or WT.

| MINITAB COMMANDS FOR BOX 15.4(a) Explaining FOREARM using HT | |
|--|---|
| Commands | <code>glm FOREARM = HT;</code> <code>covariate HT;</code> <code>brief 1.</code> |

Menu route

Stat > ANOVA > General Linear Model

FOREARM → Response

HT → Model

Covariates...

HT → Covariates

Results...

⊙ Analysis of variance table

MINITAB OUTPUT FOR BOX 15.4(a) FOREARM = HT

General Linear Model: FOREARM versus

Factor Type Levels Values

Analysis of Variance for FOREARM, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|--------|----|---------|---------|--------|------|-------|
| HT | 1 | 0.944 | 0.944 | 0.944 | 0.18 | 0.678 |
| Error | 37 | 199.094 | 199.094 | 5.381 | | |
| Total | 38 | 200.038 | | | | |

MINITAB COMMANDS FOR BOX 15.4(b) **Explaining** FOREARM using WT

Commands

```
glm FOREARM = WT;
covariate WT;
brief 1.
```

Menu route

Stat > ANOVA > General Linear Model

FOREARM → Response

WT → Model

Covariates...

WT → Covariates

Results...

⊙ Analysis of variance table

| MINITAB OUTPUT FOR BOX 15.4(b) FOREARM = WT | | | | | | |
|---|------|---------|---------|--------|-------|-------|
| General Linear Model: FOREARM versus | | | | | | |
| Factor | Type | Levels | Values | | | |
| Analysis of Variance for FOREARM, using Adjusted SS for Tests | | | | | | |
| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
| WT | 1 | 59.137 | 59.137 | 59.137 | 15.53 | 0.000 |
| Error | 37 | 140.901 | 140.901 | 3.808 | | |
| Total | 38 | 200.038 | | | | |

Then the joint analysis has to be conducted using both explanatory variables.

| MINITAB COMMANDS FOR BOX 15.5 Using both HT and WT to explain FOREARM | |
|---|---|
| Commands | glm FOREARM = HT + WT; covariate HT WT; brief 3. |
| Menu route | Stat > ANOVA > General Linear Model FOREARM → Response HT WT → Model Covariates... HT WT → Covariates Results... ⊙ In addition, coefficients for all terms. |

| MINITAB OUTPUT FOR BOX 15.5 FOREARM = HT + WT | | | | | | |
|---|------|----------|---------|--------|-------|-------|
| General Linear Model: FOREARM versus | | | | | | |
| Factor | Type | Levels | Values | | | |
| Analysis of Variance for FOREARM, using Adjusted SS for Tests | | | | | | |
| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
| HT | 1 | 0.944 | 24.777 | 24.777 | 7.68 | 0.009 |
| WT | 1 | 82.970 | 82.970 | 82.970 | 25.72 | 0.000 |
| Error | 36 | 116.124 | 116.124 | 3.226 | | |
| Total | 38 | 200.038 | | | | |
| Term | | Coef | SE Coef | T | | P |
| Constant | | 17.452 | 8.274 | 2.11 | | 0.042 |
| HT | | -0.17173 | 0.06196 | -2.77 | | 0.009 |
| WT | | 0.23317 | 0.04598 | 5.07 | | 0.000 |

Unusual Observations for FOREARM

| Obs | FOREARM | Fit | SE Fit | Residual | St Resid |
|-----|---------|---------|---------|----------|----------|
| 7 | 7.74100 | 3.66338 | 0.48987 | 4.07762 | 2.36R |
| 9 | 0.23200 | 2.20161 | 0.89018 | -1.96961 | -1.26 X |
| 10 | 9.81100 | 9.79442 | 1.12860 | 0.01658 | 0.01 X |
| 37 | 8.58200 | 3.67800 | 0.48285 | 4.90400 | 2.83R |

R denotes an observation with a large standardized residual.

X denotes an observation whose X value gives it large influence.

Chapter 5

The dorsal crest of the male smooth newt

In the first analysis you are asked to investigate the relationship between LCREST and the body size of the newt. The response variable you are given is logged, therefore, the body size variable should also be logged. The commands and menus are given below.

MINITAB COMMANDS FOR BOX 15.6 Dorsal crest analysis

Commands

```
glm LCREST = LSVL;
covariate LSVL;
brief 3.
```

Menu route

```
Stat > ANOVA > General Linear Model
LCREST → Response
LSVL → Model
```

Covariates...

LSVL → Covariates

Results...

⊙ In addition, coefficients for all terms.

This would result in the following output:

| MINITAB OUTPUT FOR BOX 15.6 Dorsal crest analysis | | | | | | |
|--|---------|---------|---------|----------|-------|----------|
| General Linear Model: LCREST versus | | | | | | |
| Factor | Type | Levels | Values | | | |
| Analysis of Variance for LCREST, using Adjusted SS for Tests | | | | | | |
| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
| LSVL | 1 | 2.3894 | 2.3894 | 2.3894 | 45.81 | 0.000 |
| Error | 85 | 4.4337 | 4.4337 | 0.0522 | | |
| Total | 86 | 6.8231 | | | | |
| Term | | Coef | SE Coef | T | | P |
| Constant | | -9.381 | 1.501 | -6.25 | | 0.000 |
| LSVL | | 5.0870 | 0.7516 | 6.77 | | 0.000 |
| Unusual Observations for LCREST | | | | | | |
| Obs | LCREST | Fit | SE Fit | Residual | | St Resid |
| 27 | 0.45700 | 0.92565 | 0.03267 | -0.46865 | | -2.07R |
| 29 | 0.49800 | 1.04774 | 0.04662 | -0.54974 | | -2.46R |
| 41 | 0.97200 | 0.51361 | 0.04626 | 0.45839 | | 2.05R |
| 46 | 1.38800 | 0.90531 | 0.03077 | 0.48269 | | 2.13R |
| 67 | 1.25400 | 0.73235 | 0.02545 | 0.52165 | | 2.30R |
| 86 | 0.12000 | 0.59500 | 0.03661 | -0.47500 | | -2.11R |
| R denotes an observation with a large standardized residual. | | | | | | |

In the second analysis, POND is also included.

| MINITAB COMMANDS FOR BOX 15.7 Further dorsal crest analysis | |
|---|--|
| Commands | <pre>glm LCREST = POND + LSVL; covariate LSVL; brief 3.</pre> |
| Menu route | <pre>Stat > ANOVA > General Linear Model LCREST → Response POND + LSVL → Model Covariates... LSVL → Covariates Results... Ⓞ Analysis of variance table</pre> |

MINITAB OUTPUT FOR BOX 15.7 Further dorsal crest analysis

General Linear Model: LCREST versus POND

| Factor | Type | Levels | Values |
|--------|-------|--------|----------------------|
| POND | fixed | 10 | 1 2 3 4 5 6 7 8 9 10 |

Analysis of Variance for LCREST, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|--------|----|---------|---------|---------|-------|-------|
| POND | 9 | 0.32519 | 0.24063 | 0.02674 | 0.48 | 0.881 |
| LSVL | 1 | 2.30483 | 2.30483 | 2.30483 | 41.78 | 0.000 |
| Error | 76 | 4.19310 | 4.19310 | 0.05517 | | |
| Total | 86 | 6.82312 | | | | |

Chapter 6

Determinants of the Grade Point Average

This exercise uses the *grades* dataset.

MINITAB COMMANDS FOR BOX 15.8 Analysis of the *grades* dataset

Commands

```
glm GPA = YEAR + VERBAL + MATH;
covariate VERBAL MATH;
brief 3.
```

Menu route

```
Stat > ANOVA > General Linear Model
GPA → Response
YEAR + VERBAL + MATH → Model
```

Covariates...

VERBAL MATH → Covariates

Results...

⊙ In addition, coefficients for all terms

MINITAB OUTPUT FOR BOX 15.8 Analysis of the *grades* dataset

General Linear Model: GPA versus YEAR

| Factor | Type | Levels | Values |
|--------|-------|--------|--------|
| YEAR | fixed | 2 | 1 2 |

Analysis of Variance for GPA, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|--------|-----|---------|---------|--------|-------|-------|
| YEAR | 1 | 1.1552 | 0.8460 | 0.8460 | 2.84 | 0.094 |
| VERBAL | 1 | 6.7595 | 5.1600 | 5.1600 | 17.32 | 0.000 |
| MATH | 1 | 0.7092 | 0.7092 | 0.7092 | 2.38 | 0.124 |
| Error | 196 | 58.3961 | 58.3961 | 0.2979 | | |
| Total | 199 | 67.0200 | | | | |

| Term | Coef | SE Coef | T | P |
|----------|----------|----------|------|-------|
| Constant | 0.6582 | 0.4404 | 1.49 | 0.137 |
| YEAR | | | | |
| 1 | 0.06521 | 0.03870 | 1.69 | 0.094 |
| VERBAL | 0.002288 | 0.000550 | 4.16 | 0.000 |
| MATH | 0.000937 | 0.000608 | 1.54 | 0.124 |

Unusual Observations for GPA

| Obs | GPA | Fit | SE Fit | Residual | St Resid |
|-----|---------|---------|---------|----------|----------|
| 40 | 1.20000 | 2.50174 | 0.09097 | -1.30174 | -2.42R |
| 54 | 2.40000 | 2.49136 | 0.13968 | -0.09136 | -0.17 X |
| 89 | 2.40000 | 2.11378 | 0.13702 | 0.28622 | 0.54 X |
| 121 | 1.30000 | 3.02639 | 0.11306 | -1.72639 | -3.23R |
| 131 | 0.30000 | 2.48641 | 0.05853 | -2.18641 | -4.03R |
| 136 | 1.10000 | 2.99751 | 0.10492 | -1.89751 | -3.54R |

R denotes an observation with a large standardized residual.

X denotes an observation whose X value gives it large influence.

Chapter 7

Weight, fat, and sex

This question requires a factorial analysis, with an interaction between a categorical and continuous explanatory variable.

MINITAB COMMANDS FOR BOX 15.9 Analysis for weight, fat, and sex

Commands `glm FAT = SEX|WEIGHT;`
 `covariate WEIGHT;`
 `brief 3.`

Menu route `Stat > ANOVA > General Linear Model`
 `FAT → Response`
 `SEX|WEIGHT → Model`
 `Covariates...`
 `WEIGHT → Covariates`
 `Results...`

⊙ In addition, coefficients for all terms.

MINITAB OUTPUT FOR BOX 15.9 Analysis for weight, fat, and sex

General Linear Model: FAT versus SEX

| Factor | Type | Levels | Values |
|--------|-------|--------|--------|
| SEX | fixed | 2 | 1 2 |

Analysis of Variance for FAT, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|------------|----|---------|--------|--------|-------|-------|
| SEX | 1 | 90.321 | 2.108 | 2.108 | 1.05 | 0.322 |
| WEIGHT | 1 | 87.105 | 79.542 | 79.542 | 39.59 | 0.000 |
| SEX*WEIGHT | 1 | 10.857 | 10.857 | 10.857 | 5.40 | 0.035 |
| Error | 15 | 30.138 | 30.138 | 2.009 | | |
| Total | 18 | 218.421 | | | | |

| Term | Coef | SE Coef | T | P |
|------------|---------|---------|-------|-------|
| Constant | 8.405 | 3.091 | 2.72 | 0.016 |
| SEX | | | | |
| 1 | -3.166 | 3.091 | -1.02 | 0.322 |
| WEIGHT | 0.29420 | 0.04676 | 6.29 | 0.000 |
| WEIGHT*SEX | | | | |
| 1 | 0.10869 | 0.04676 | 2.32 | 0.035 |

Unusual Observations for FAT

| Obs | GPA | Fit | SE Fit | Residual | St Resid |
|-----|---------|---------|--------|----------|----------|
| 16 | 26.0000 | 29.0103 | 0.5912 | -3.0103 | -2.34R |

R denotes an observation with a large standardized residual.

Chapter 8

Combining data from different experiments

MINITAB COMMANDS FOR BOX 15.11 Bird data combined

Commands `glm YOUNG = YEAR + SONGDAY;`
 `covariate SONGDAY;`
 `brief 3.`

Menu route Stat > ANOVA > General Linear Model
 YOUNG → Response
 YEAR + SONGDAY → Model

Covariates...

 SONGDAY → Covariates

Results...

⊙ In addition, coefficients for all terms

MINITAB OUTPUT FOR BOX 15.11 Bird data combined

General Linear Model: YOUNG versus YEAR

| Factor | Type | Levels | Values |
|--------|-------|--------|-----------|
| YEAR | fixed | 5 | 1 2 3 4 5 |

Analysis of Variance for YOUNG, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|---------|----|--------|--------|--------|-------|-------|
| YEAR | 4 | 10.698 | 19.782 | 4.945 | 4.06 | 0.008 |
| SONGDAY | 1 | 12.202 | 12.202 | 12.202 | 10.02 | 0.003 |
| Error | 38 | 46.282 | 46.282 | 1.218 | | |
| Total | 43 | 69.182 | | | | |

| Term | Coef | SE Coef | T | P |
|----------|----------|---------|-------|-------|
| Constant | 5.4922 | 0.8637 | 6.36 | 0.000 |
| YEAR | | | | |
| 1 | 0.1776 | 0.3746 | 0.47 | 0.638 |
| 2 | 1.4089 | 0.3772 | 3.73 | 0.001 |
| 3 | -0.4916 | 0.4761 | -1.03 | 0.308 |
| 4 | 0.4453 | 0.3998 | 1.11 | 0.272 |
| SONGDAY | -0.10913 | 0.03448 | -3.17 | 0.003 |

Unusual Observations for YOUNG

| Obs | YOUNG | Fit | SE Fit | Residual | St Resid |
|-----|---------|---------|---------|----------|----------|
| 20 | 7.00000 | 3.84557 | 0.33677 | 3.15443 | 3.00R |
| 22 | 5.00000 | 2.92715 | 0.43223 | 2.07285 | 2.04R |
| 28 | 1.00000 | 3.14541 | 0.41947 | -2.14541 | -2.10R |

R denotes an observation with a large standardized residual.

Chapter 9

Stabilising the variance in a blocked experiment

The commands required for the first part of this exercise (a) transform the data; (b) perform the analysis on the transformed data, storing the residuals and plotting the residuals against the fitted values; (c) display descriptive statistics for the residuals by treatment.

MINITAB COMMANDS FOR BOXES 15.12 AND 15.13, AND FIG. 15.6

Commands

```
name C4 = 'SQRTNCOT'
let SQRTNCOT = SQRT(NCOT)

name c5 = 'SRES1'

glm SQRTNCOT = BLOCK + TRTMNT;
brief 1;
sresiduals SRES1;
gfits;
rtype 2.

describe SRES1;
by TRTMNT.
```

Menu route

```
Calc > Calculator
    SQRTNCOT → Store result in variable
    SQRT(NCOT) → Expression

Stat > ANOVA > General Linear Model
    SQRTNCOT → Responses
    BLOCK + TRTMNT → Model

    Results...
        ☉ Analysis of variance table.

    Graphs...
        ☉ In addition, coefficients for all terms.
        ☑ Residuals versus fits
```

Storage...

Standardised residuals

Stat > Basic Statistics > Display Descriptive Statistics
 SRES1 → Variables
 By variable:
 TRTMNT → By variable

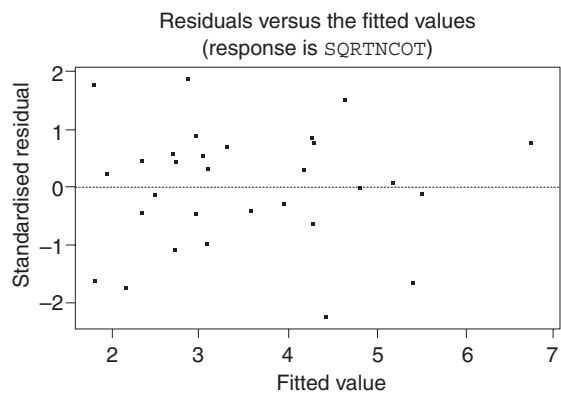
MINITAB OUTPUT FOR BOX 15.12 Analysis of blocked experiment

General Linear Model: SQRTNCOT versus BLOCK, TRTMNT

| Factor | Type | Levels | Values |
|--------|-------|--------|-------------|
| BLOCK | fixed | 6 | 1 2 3 4 5 6 |
| TRTMNT | fixed | 5 | 1 2 3 4 5 |

Analysis of Variance for SQRTNCOT, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|--------|----|---------|---------|--------|-------|-------|
| BLOCK | 5 | 23.9098 | 23.9098 | 4.7820 | 53.45 | 0.000 |
| TRTMNT | 4 | 20.5340 | 20.5340 | 5.1335 | 57.37 | 0.000 |
| Error | 20 | 1.7895 | 1.7895 | 0.0895 | | |
| Total | 29 | 46.2333 | | | | |



Minitab output for Fig. 15.6.

MINITAB OUTPUT FOR BOX 15.13: Examining residuals of the square root transform analysis

Descriptive Statistics: SRES1 by TRTMNT

| Variable | TRTMNT | N | Mean | Median | TrMean | StDev |
|----------|--------|---|--------|--------|--------|-------|
| SRES1 | 1 | 6 | -0.000 | 0.297 | -0.000 | 0.936 |
| | 2 | 6 | 0.000 | -0.108 | 0.000 | 1.091 |
| | 3 | 6 | -0.000 | -0.075 | -0.000 | 0.425 |
| | 4 | 6 | 0.000 | 0.376 | 0.000 | 1.402 |
| | 5 | 6 | 0.000 | 0.319 | 0.000 | 1.336 |

| Variable | TRTMNT | SE Mean | Minimum | Maximum | Q1 | Q3 |
|----------|--------|---------|---------|---------|--------|-------|
| SRES1 | 1 | 0.382 | -1.663 | 0.868 | -0.774 | 0.726 |
| | 2 | 0.446 | -1.096 | 1.869 | -1.017 | 0.793 |
| | 3 | 0.173 | -0.443 | 0.557 | -0.422 | 0.479 |
| | 4 | 0.573 | -1.744 | 1.767 | -1.651 | 1.076 |
| | 5 | 0.545 | -2.255 | 1.498 | -1.048 | 0.947 |

These commands can then be repeated for the log and inverse transformation.

Checking the 'perfect' model

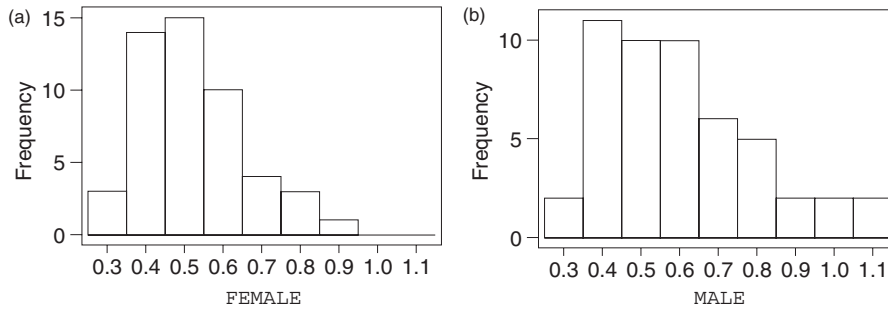
The commands to produce the histograms of the original and transformed data are reproduced below. We specify 'MidPoints' so that Minitab will use the same scale on the x-axes, making the histograms easier to compare by eye.

MINITAB COMMANDS TO PRODUCE FIG. 15.9a AND b

Commands histogram MALE FEMALE;
 midpoint 0.3:1.1/0.1.

Menu route Graph > Histogram
 MALE → Graph variables, X row 1
 FEMALE → Graph variables, X row 2

 Midpoint/cutpoint positions:
 0.3:1.1/0.1 → Midpoint/cutpoint positions



Minitab output for Fig. 15.9a and b.

MINITAB COMMANDS TO PRODUCE FIG. 15.9c AND d

Commands

```

name C3 = 'LMALE'
let LMALE = LOGE (MALE)
name C4 = 'LFEM'
let LFEM = LOGE (FEMALE)
histogram LMALE LFEM;
midpoint -1.2:0.1/0.1.
    
```

Menu route

Calc > Calculator

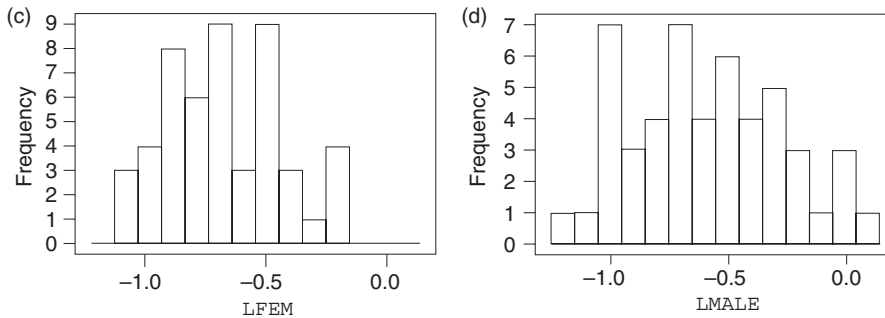
- LMALE → Store result in variable
- LOGE (MALE) → Expression
- LFEM → Store result in variable
- LOGE (FEMALE) → Expression

Graph > Histogram

- LMALE → Graph variables, X row 1
- LFEM → Graph variables, X row 2

Options...

- Midpoint/cutpoint positions.
- 1.2:0.1/0.1. → Midpoint/cutpoint positions

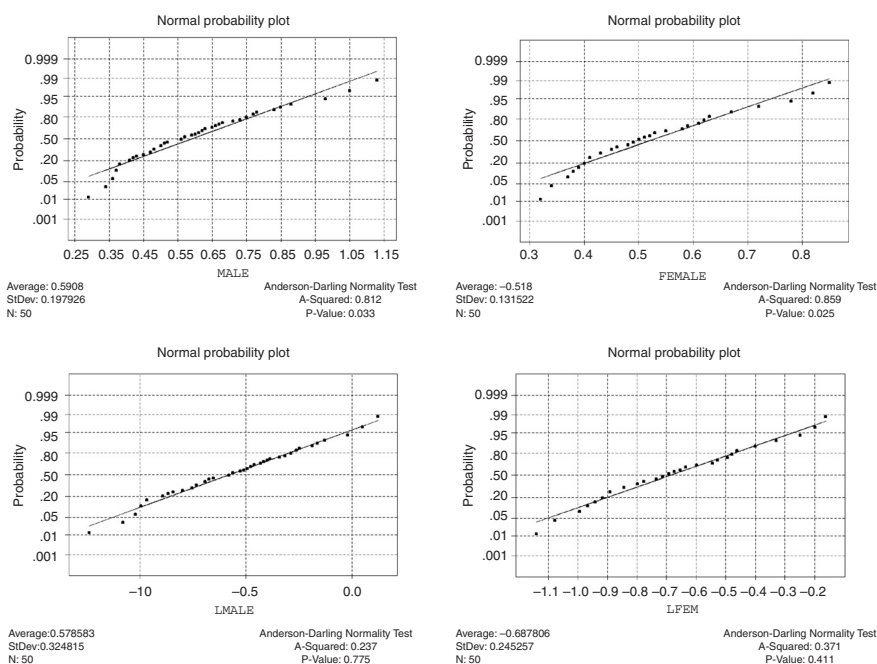


Minitab output for Fig. 15.9c and d.

The Normal probability plot may not only be performed as part of a GLM analysis (see earlier this chapter), but may also be performed on raw data using a different set of commands, for example:

| MINITAB COMMANDS FOR FIG. 15.10: Normal Probability Plots | |
|---|---|
| Commands | <code>%normplot 'MALE'.</code> |
| Menu route | Graph > Probability plot > Normality Test MALE → Variables |

This may be repeated for the other three variables, producing the graphs below.



Minitab output for Fig. 15.10 Normal probability plots

Minitab provides a p -value associated with the Anderson–Darling Normality test (this is the test chosen by default), which can provide us with a criterion for rejecting the assumption of Normality. The p -value is below 0.05 for the raw data, but not for the transformed data.

The following commands allow you to create the null datasets designed to follow a Normal distribution, with a mean and standard deviation equal to that of the female squirrel weights (which can be obtained using the describe command, as used earlier).

MINITAB COMMANDS TO CREATE NORMALLY DISTRIBUTED NULL DATASETS

| | |
|------------|---|
| Commands | <pre>name c5 = 'SIMFEM1' random 50 SIMFEM1; normal 0.518 0.1315.</pre> |
| Menu route | <pre>Calc > Random Data > Normal 50 → Generate ... rows of data SIMFEM1 → store in columns 0.518 → mean 0.1315 → standard deviation</pre> |

This can be repeated to create as many columns of simulated female (or male) data as you require. This is particularly easy using the written commands in the session window, as one can copy-and-paste the relevant commands. These may then be examined using the histogram and Normal probability plot commands used earlier.

Chapter 10

Partitioning a sum of squares into polynomial components

The following commands are required for this exercise. Note that in the command language the analysis is conducted in two parts. In the first part, the 'interaction means' are stored at the same time as conducting the ANOVA and printing out a table of means. In the second part, a Minitab macro is called upon to draw the interaction diagram.

MINITAB COMMANDS FOR BOX 15.18 AND FIG. 10.8 Analysis for barley yield

| | |
|----------|---|
| Commands | <pre>glm BYIELD = BBLOCK + BSPACE BVARIETY; brief 1; means BSPACE*BVARIETY; smeans c4000; interact BVARIETY BSPACE. %gfint 'BVARIETY' 'BSPACE'; responses 'BYIELD'; lsmeans c4000.</pre> |
|----------|---|

Menu route Stat > ANOVA > General Linear Model
 BYIELD → Response
 BBLOCK + BSPACE|BVARIETY → Model

Results...

⊙ Analysis of variance table
 BSPACE*BVARIETY → Display least squares means corresponding to the terms

Factor Plots...

BVARIETY BSPACE → Interactions Plot, Factors:

MINITAB OUTPUT FOR BOX 15.18 Analysis for barley yield

General Linear Model: BYIELD versus BBLOCK, BSPACE, BVARIETY

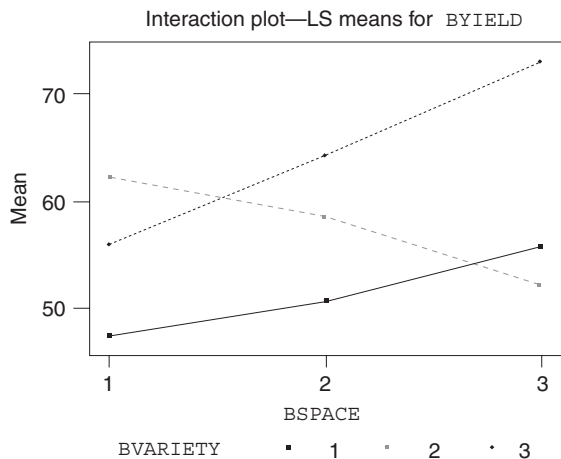
| Factor | Type | Levels | Values |
|----------|-------|--------|---------|
| BBLOCK | fixed | 4 | 1 2 3 4 |
| BSPACE | fixed | 3 | 1 2 3 |
| BVARIETY | fixed | 3 | 1 2 3 |

Analysis of Variance for BYIELD, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|-----------------|----|---------|---------|--------|-------|-------|
| BBLOCK | 3 | 255.64 | 255.64 | 85.21 | 4.82 | 0.009 |
| BSPACE | 2 | 155.06 | 155.06 | 77.53 | 4.39 | 0.024 |
| BVARIETY | 2 | 1027.39 | 1027.39 | 513.69 | 29.07 | 0.000 |
| BSPACE*BVARIETY | 4 | 765.44 | 765.44 | 191.36 | 10.83 | 0.000 |
| Error | 24 | 424.11 | 424.11 | 17.67 | | |
| Total | 35 | 2627.64 | | | | |

p[Least Squares Means for BYIELD

| BSPACE*BVARIETY | | Mean | SE Mean |
|-----------------|---|-------|---------|
| 1 | 1 | 47.50 | 2.102 |
| 1 | 2 | 62.25 | 2.102 |
| 1 | 3 | 56.00 | 2.102 |
| 2 | 1 | 50.75 | 2.102 |
| 2 | 2 | 58.50 | 2.102 |
| 2 | 3 | 64.25 | 2.102 |
| 3 | 1 | 55.75 | 2.102 |
| 3 | 2 | 52.25 | 2.102 |
| 3 | 3 | 73.00 | 2.102 |



Minitab output for Fig. 10.8 Interaction diagram from the *barley* dataset.

A second analysis is then conducted on the *barley* dataset, involving a polynomial decomposition. We choose to include the interaction of BVARIETY with the quadratic term BSPACE*BSPACE so that the polynomial analysis is a decomposition of the non-polynomial analysis. This means that the error SS, MS, and DF will be the same in the two analyses, allowing us to compare them more easily. It also allows us to investigate whether the response of yield to spacing is curvilinear for some varieties but not others.

| MINITAB COMMANDS FOR BOX 15.19 Second analysis for barley yield | |
|---|---|
| Commands | <pre>glm BYIELD = BBLOCK + BVARIETY BSPACE BSPACE; covariate BSPACE; brief 1; ssquares 1.</pre> |
| Menu route | <pre>Stat > ANOVA > General Linear Model BYIELD → Response BBLOCK + BVARIETY BSPACE BSPACE → Model Covariates... BSPACE → Covariates Results... ⊙ Analysis of variance table Options... ⊙ Sequential (Type I)</pre> |

MINITAB OUTPUT FOR BOX 15.19 Second analysis for barley yield

General Linear Model: BYIELD versus BBLOCK, BVARIETY

| Factor | Type | Levels | Values |
|----------|-------|--------|---------|
| BBLOCK | fixed | 4 | 1 2 3 4 |
| BVARIETY | fixed | 3 | 1 2 3 |

Analysis of Variance for SQRNCOT, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|------------------------|----|---------|--------|--------|-------|-------|
| BBLOCK | 3 | 255.64 | 255.64 | 85.21 | 4.82 | 0.009 |
| BVARIETY | 2 | 1027.39 | 38.17 | 513.69 | 29.07 | 0.000 |
| BSPACE | 1 | 155.04 | 3.59 | 155.04 | 8.77 | 0.007 |
| BVARIETY*BSPACE | 2 | 759.08 | 5.65 | 379.54 | 21.48 | 0.000 |
| BSPACE*BSPACE | 1 | 0.01 | 0.01 | 0.01 | 0.00 | 0.978 |
| BVARIETY*BSPACE*BSPACE | 2 | 6.36 | 6.36 | 3.18 | 0.18 | 0.836 |
| Error | 24 | 424.11 | 424.11 | 17.67 | | |
| Total | 35 | 2627.64 | | | | |

Chapter 11**Finding the best treatment for cat fleas**

The final model is:

MINITAB COMMANDS FOR BOX 15.20 Analysis for cat fleas

Commands

```
glm LOGFLEAS = TRTMT + NCATS + CARPET;
covariates NCATS;
brief 1.
```

Menu route

```
Stat > ANOVA > General Linear Model
LOGFLEAS → Response
TRTMT + NCATS + CARPET → Model
```

Results...

⊙ Analysis of variance table

Covariates...

NCATS → Covariates

| MINITAB OUTPUT FOR BOX 15.20 Analysis for cat fleas | | | | | | |
|--|-------|--------|--------|--------|-------|-------|
| General Linear Model: LOGFLEAS versus TRTMT, CARPET | | | | | | |
| Factor | Type | Levels | Values | | | |
| TRTMT | fixed | 2 | 1 2 | | | |
| CARPET | fixed | 2 | 1 2 | | | |
| Analysis of Variance for LOGFLEAS, using Adjusted SS for Tests | | | | | | |
| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
| TRTMT | 1 | 1.612 | 5.750 | 5.750 | 9.09 | 0.003 |
| NCATS | 1 | 23.730 | 22.962 | 22.962 | 36.31 | 0.000 |
| CARPET | 1 | 6.103 | 6.103 | 6.103 | 9.65 | 0.003 |
| Error | 85 | 53.759 | 53.759 | 0.632 | | |
| Total | 88 | 85.203 | | | | |

Multiplicity of p values

To create the random dataset:

| MINITAB COMMANDS TO PRODUCE THE NULL DATASET | |
|--|---|
| Commands | random 30 c1-c11; normal 10.5 2.4. |
| Menu route | Calc > Random Data > Normal 30 → Generate ... rows of data C1-C11 → Store in columns 10.5 → Mean 2.4 → Standard deviation |

Using the regression menu would provide output giving the p value for the regression as a whole, with the p values for each individual X variable in the analysis being found in the table of coefficients. (The p -value resulting from the t test for the slope against zero for a particular variable is the same as the p -value for the F ratio test for the same explanatory variable in the analysis of variance table. This arises from the fact that $t^2 = F$; see Appendix 3.)

MINITAB COMMANDS TO PRODUCE OUTPUT FOR TABLE 15.6

Commands regress C1 10 C2-C11;
 brief 1.

Menu route Stat > Regression > Regression
 C1 → Response
 C2-C11 → Predictors

Predictors...

⊙ Regression equation, table of coefficients,
s, R-squared and basic analysis of variance.

EXAMPLE MINITAB OUTPUT FOR TABLE 15.6

Regression Analysis: C1 versus C2, C3, C4, C5, C6, C7, C8, C9, C10, C11

The regression equation is

$C1 = 8.48 + 0.006 C2 + 0.333 C3 - 0.016 C4 - 0.219 C5 - 0.063 C6 - 0.038 C7 + 0.206 C8 - 0.152 C9 + 0.217 C10 - 0.078 C11$

| Predictor | Coef | SE Coef | T | P |
|-----------|---------|---------|-------|-------|
| Constant | 8.478 | 6.481 | 1.31 | 0.206 |
| C2 | 0.0064 | 0.1739 | 0.04 | 0.971 |
| C3 | 0.3328 | 0.1750 | 1.90 | 0.072 |
| C4 | -0.0164 | 0.1604 | -0.10 | 0.919 |
| C5 | -0.2187 | 0.1401 | -1.56 | 0.135 |
| C6 | -0.0627 | 0.1383 | -0.45 | 0.655 |
| C7 | -0.0377 | 0.1950 | -0.19 | 0.849 |
| C8 | 0.2061 | 0.1291 | 1.60 | 0.127 |
| C9 | -0.1520 | 0.1611 | -0.94 | 0.357 |
| C10 | 0.2167 | 0.2086 | 1.04 | 0.312 |
| C11 | -0.0784 | 0.1847 | -0.42 | 0.676 |

S = 1.813

R-Sq = 41.6%

R-Sq(adj) = 10.9%

Analysis of Variance

| Source | DF | SS | MS | F | P |
|----------------|----|---------|-------|------|-------|
| Regression | 10 | 44.587 | 4.459 | 1.36 | 0.272 |
| Residual Error | 19 | 62.467 | 3.288 | | |
| Total | 29 | 107.054 | | | |

Chapter 12

How a nested analysis can solve problems of non-independence

These commands first calculate the variable LUPRATE, and then conduct a nested analysis.

MINITAB COMMANDS FOR BOX 15.21 Nested analysis of *sheep* dataset

| | |
|------------|---|
| Commands | <pre>name C6 = 'LUPRATE'. let LUPRATE = NLOOKUPS / DURATION. glm LUPRATE = SEX + SHEEP(SEX); random SHEEP; brief 1; ems.</pre> |
| Menu route | <p>Calc > Calculator LUPRATE → Store result in variable NLOOKUPS / DURATION → Expression:</p> <p>Stat > ANOVA > General Linear Model LUPRATE → Response SEX + SHEEP (SEX) → Model SHEEP → Random Factors</p> <div style="border: 1px solid black; padding: 2px; display: inline-block; margin: 5px 0;">Results...</div> <ul style="list-style-type: none"> <input type="radio"/> Analysis of variance table <input checked="" type="checkbox"/> Display expected mean squares and variance components |

MINITAB OUTPUT FOR BOX 15.21 Nested analysis of *sheep* dataset

General Linear Model: LUPRATE versus SEX, SHEEP

| Factor | Type | Levels | Values |
|-------------|--------|--------|-------------|
| SEX | fixed | 2 | 1 2 |
| SHEEP (SEX) | random | 6 | 1 2 3 1 2 3 |

Analysis of Variance for LUPRATE, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|-------------|-----|----------|----------|----------|-------|-------|
| SEX | 1 | 0.132816 | 0.132816 | 0.132816 | 1.80 | 0.251 |
| SHEEP (SEX) | 4 | 0.294774 | 0.294774 | 0.073693 | 26.89 | 0.000 |
| Error | 114 | 0.312387 | 0.312387 | 0.002740 | | |
| Total | 119 | 0.739977 | | | | |

Expected Mean Squares, using Adjusted SS

| Source | Expected Mean | Square for Each Term |
|--------------|---------------|----------------------|
| 1 SEX | (3) + 20.0000 | (2) + Q[1] |
| 2 SHEEP(SEX) | (3) + 20.0000 | (2) |
| 3 Error | (3) | |

Error Terms for Tests, using Adjusted SS

| Source | Error DF | Error MS | Synthesis of Error MS |
|--------------|----------|----------|-----------------------|
| 1 SEX | 4.00 | 0.073693 | (2) |
| 2 SHEEP(SEX) | 114.00 | 0.002740 | (3) |

Variance Components, using Adjusted SS

| Source | Estimated Value |
|------------|-----------------|
| SHEEP(SEX) | 0.00355 |
| Error | 0.00274 |

Chapter 13

Fig trees in Costa Rica

MINITAB COMMANDS FOR TABLE 15.7 Means and variances for fig tree sites

| | |
|------------|---|
| Commands | describe NINDIVS; by SITE. describe NINDIVS. |
| Menu route | Stat > Basic Statistics > Display Descriptive Statistics NINDIVS → Variables <input checked="" type="checkbox"/> By variable SITE → By variable Stat > Basic Statistics > Display Descriptive Statistics NINDIVS → Variables |

MINITAB OUTPUT FOR TABLE 15.7 Means and variances for fig tree sites

Descriptive Statistics: NINDIVS by SITE

| Variable | SITE | N | Mean | Median | TrMean | StDev |
|----------|------|-----|--------|--------|--------|-------|
| NINDIVS | 1 | 100 | 9.510 | 9.500 | 9.467 | 3.218 |
| | 2 | 100 | 18.930 | 19.000 | 18.989 | 4.409 |
| | 3 | 100 | 41.430 | 41.000 | 41.422 | 6.261 |

| Variable | SITE | SE Mean | Minimum | Maximum | Q1 | Q3 |
|----------|------|---------|---------|---------|--------|--------|
| NINDIVS | 1 | 0.322 | 2.000 | 17.000 | 7.000 | 12.000 |
| | 2 | 0.441 | 8.000 | 28.000 | 16.000 | 22.000 |
| | 3 | 0.626 | 27.000 | 56.000 | 37.000 | 45.000 |

Descriptive Statistics: NINDIVS

| Variable | N | Mean | Median | TrMean | StDev | SE Mean |
|----------|-----|--------|--------|--------|--------|---------|
| NINDIVS | 300 | 23.290 | 19.000 | 22.748 | 14.239 | 0.822 |

| Variable | Minimum | Maximum | Q1 | Q3 |
|----------|---------|---------|--------|--------|
| NINDIVS | 2.000 | 56.000 | 11.000 | 37.000 |

MINITAB COMMANDS FOR BOX 15.22

Commands

```
name C6 = 'SQRTN'
let SQRTN = SQRT(NINDIVS)
glm SQRTN = SITE;
brief 1.
```

Menu route

```
Calc > Calculator
SQRTN → Store result in variable
SQRT(NINDIVS) → Expression
```

```
Stat > ANOVA > General Linear Model
SQRTN → Response
SITE → Model
```

Results...

⊙ Analysis of variance table

MINITAB OUTPUT FOR BOX 15.22

General Linear Model: SQRTN versus SITE

| Factor | Type | Levels | Values |
|--------|-------|--------|--------|
| SITE | fixed | 3 | 1 2 3 |

Analysis of Variance for SQRTN, using Adjusted SS for Tests

| Source | DF | Seq SS | Adj SS | Adj MS | F | P |
|--------|-----|--------|--------|--------|---------|-------|
| SITE | 2 | 582.63 | 582.63 | 291.31 | 1091.99 | 0.000 |
| Error | 297 | 79.23 | 79.23 | 0.27 | | |
| Total | 299 | 661.86 | | | | |